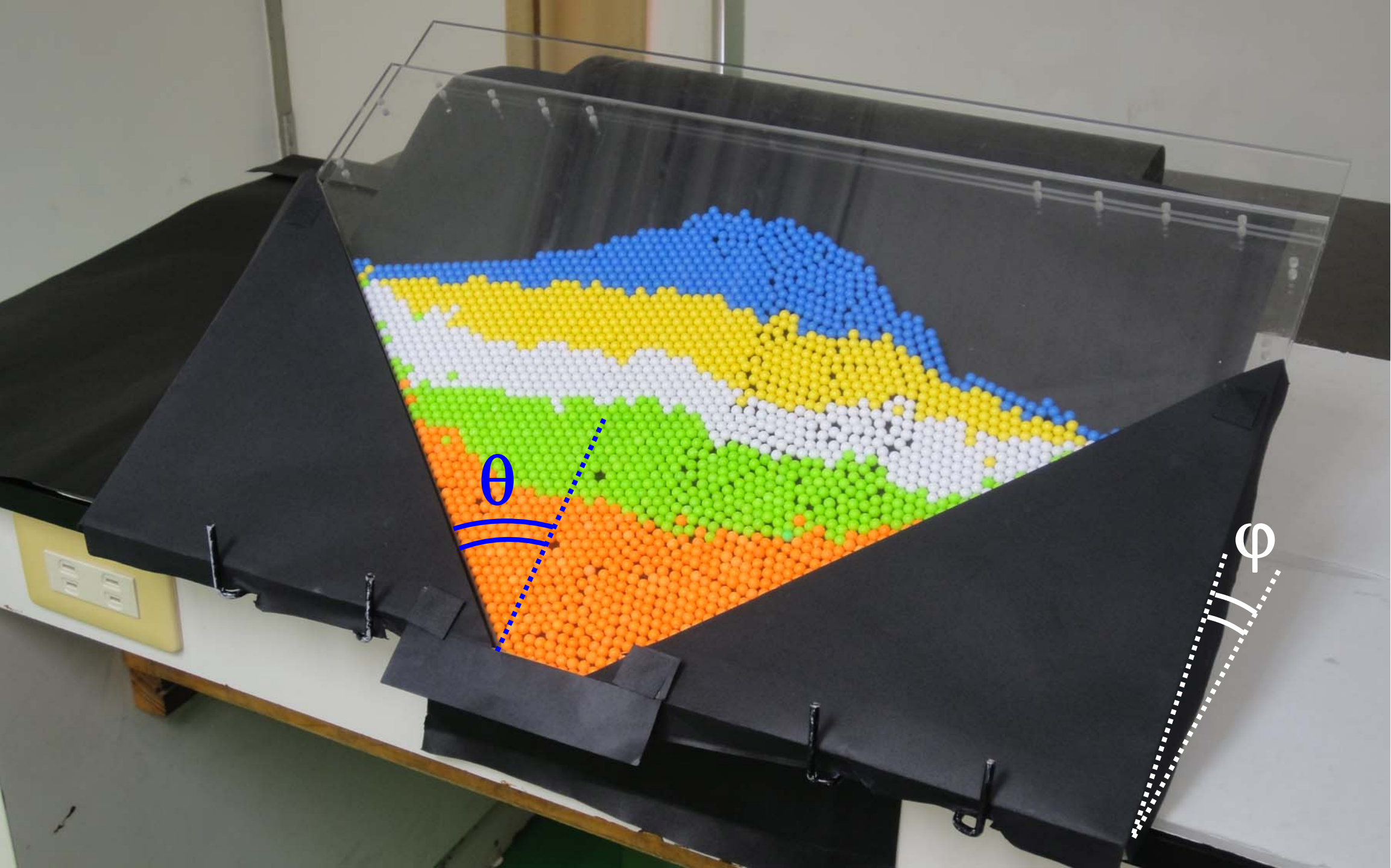


**2012 APCYS**

**Reverse Ordering in Dynamical  
Two-Dimensional Hopper Flow**

**Hao-Wen Dong and Chen-Chieh Ping**



$\theta$

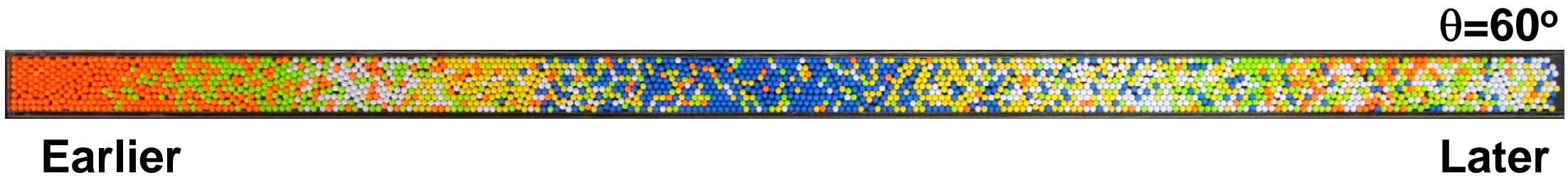
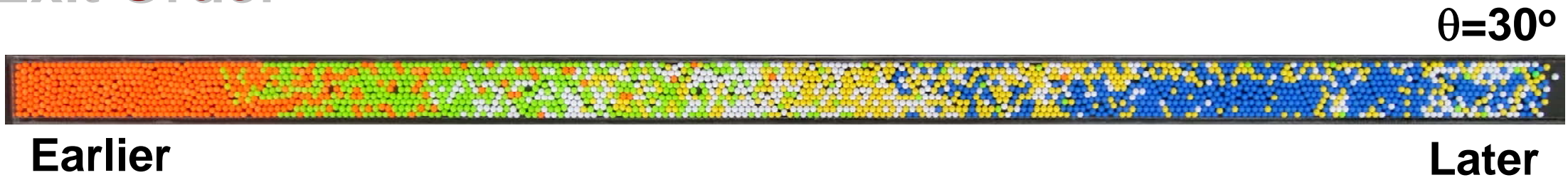
$\phi$



# Entry Order

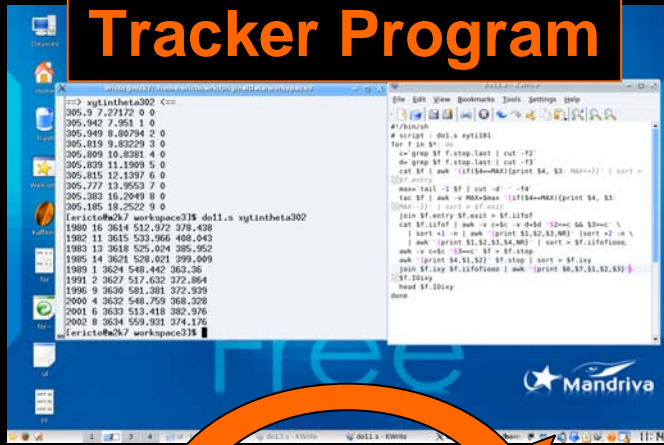


# Exit Order



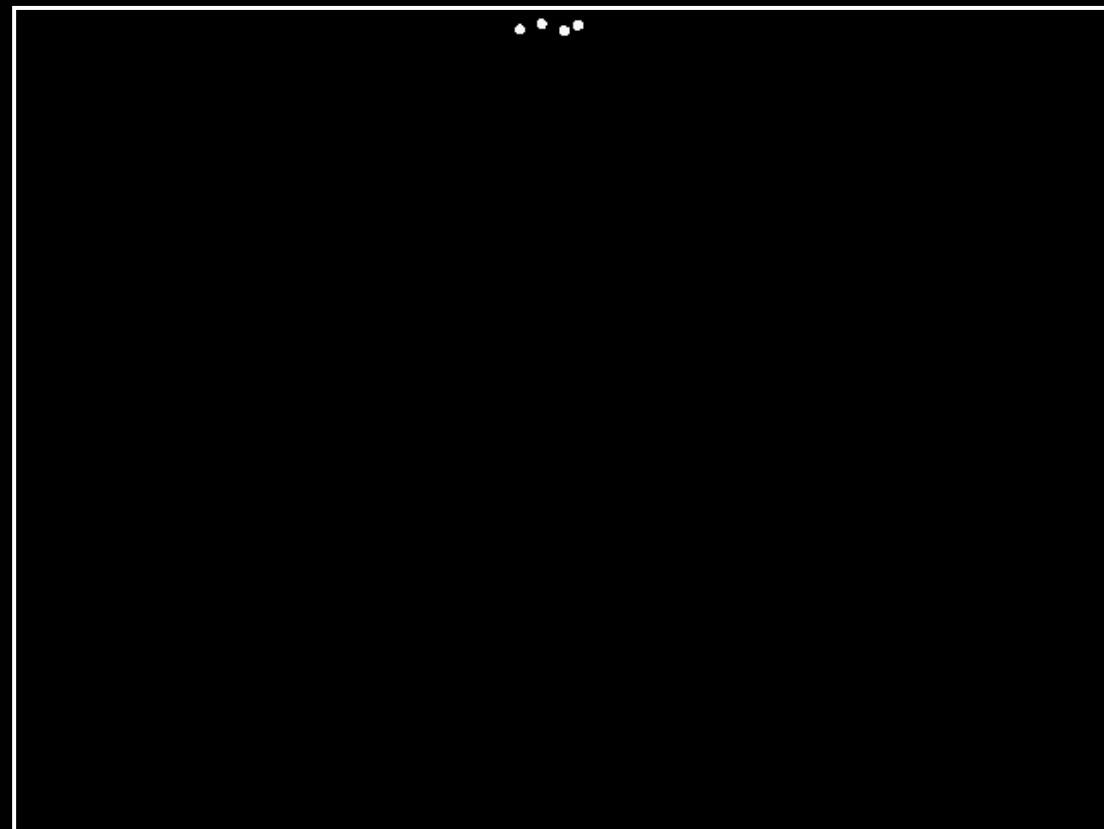
# Reverse Ordering

# Tracker Program

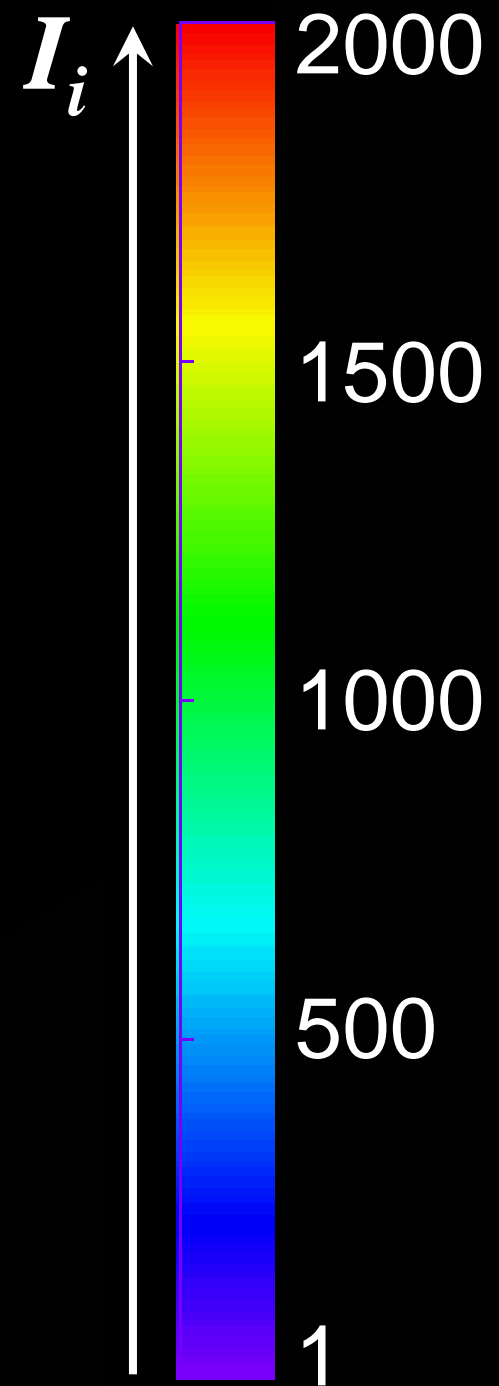


Original Video

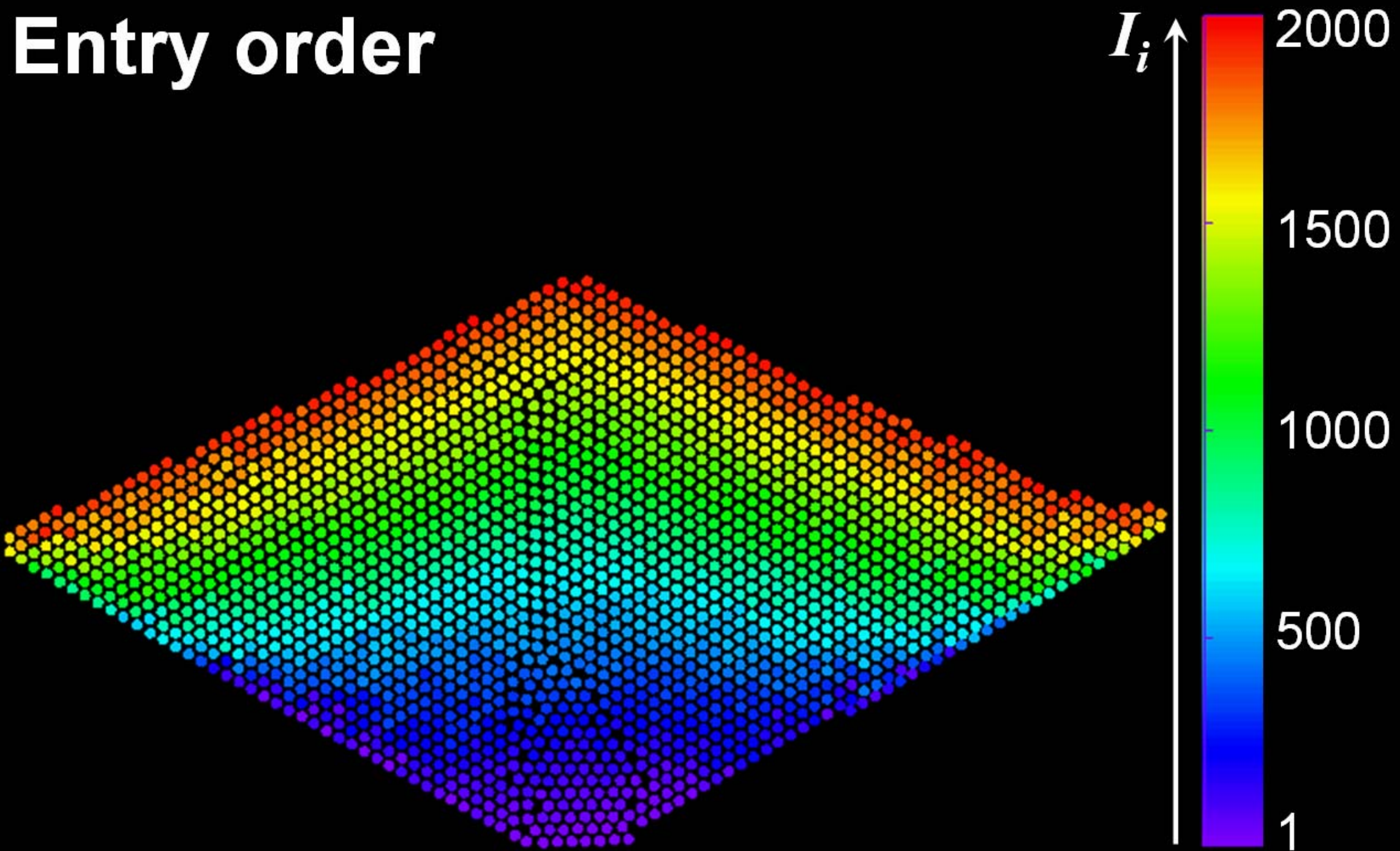
Program Output

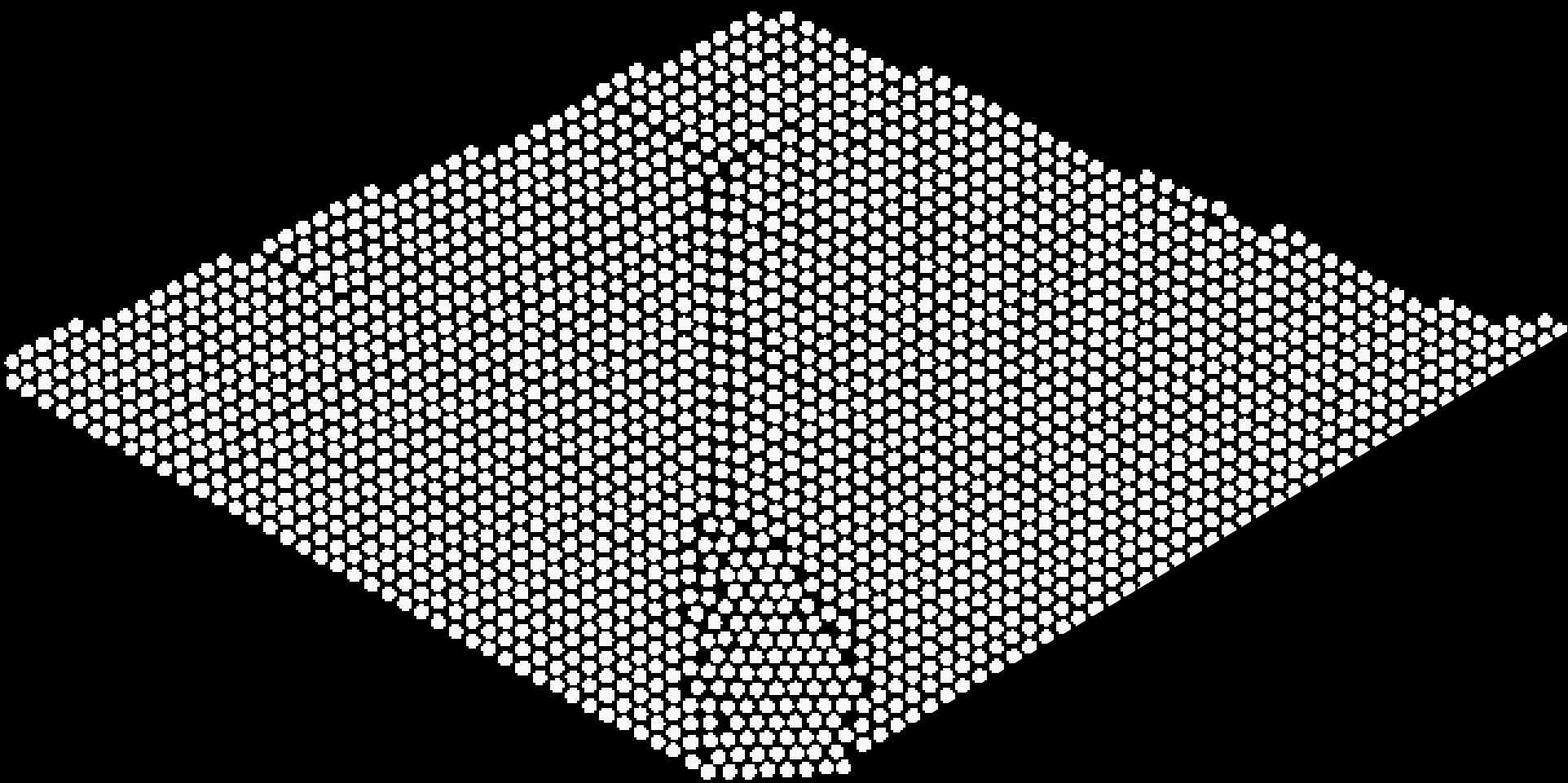


# Entry order



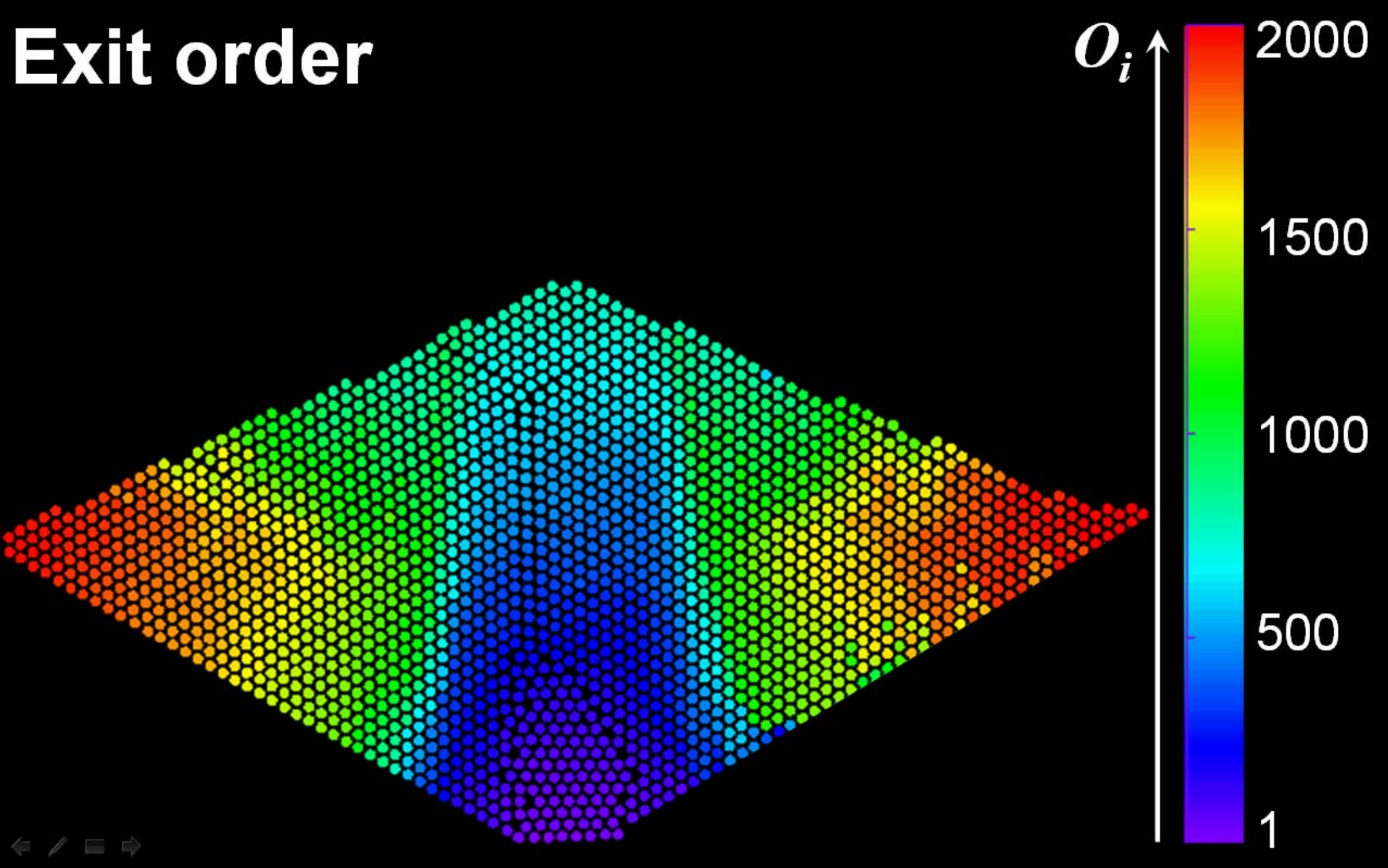
Entry order



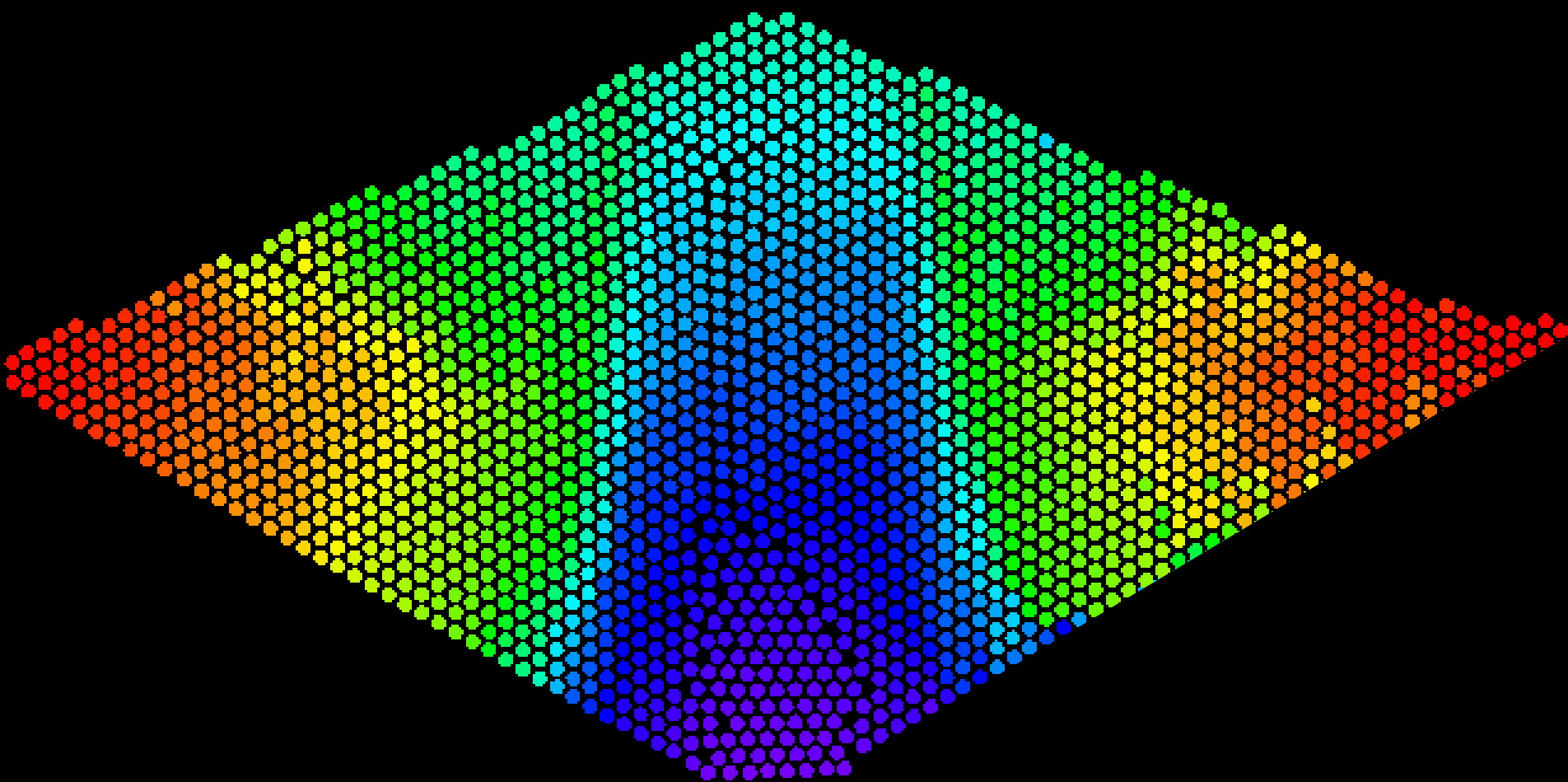
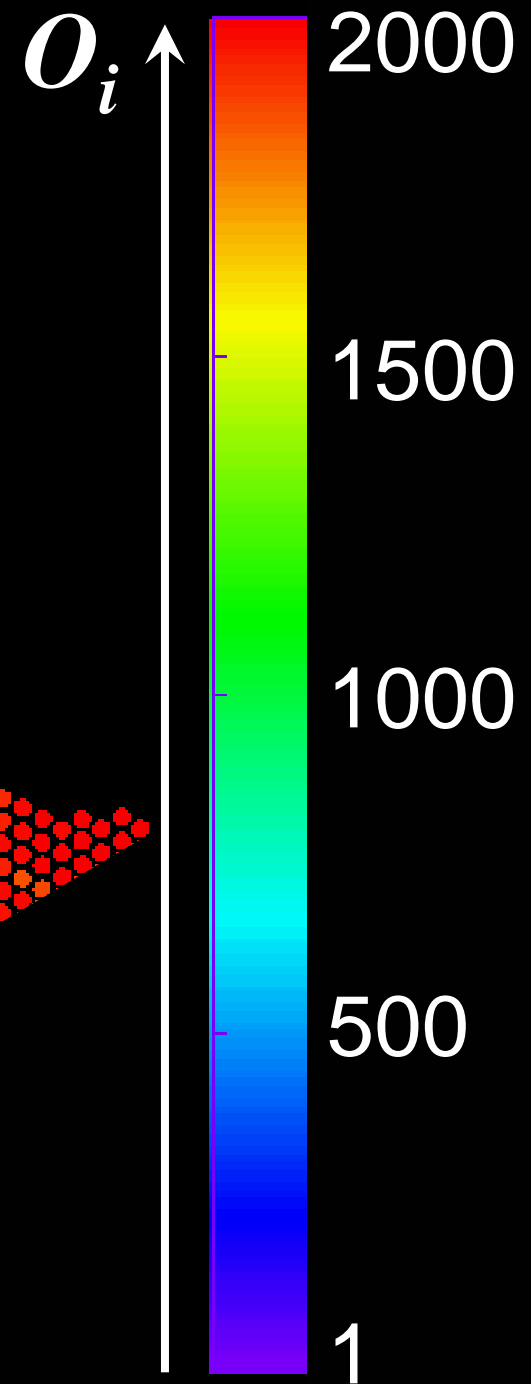


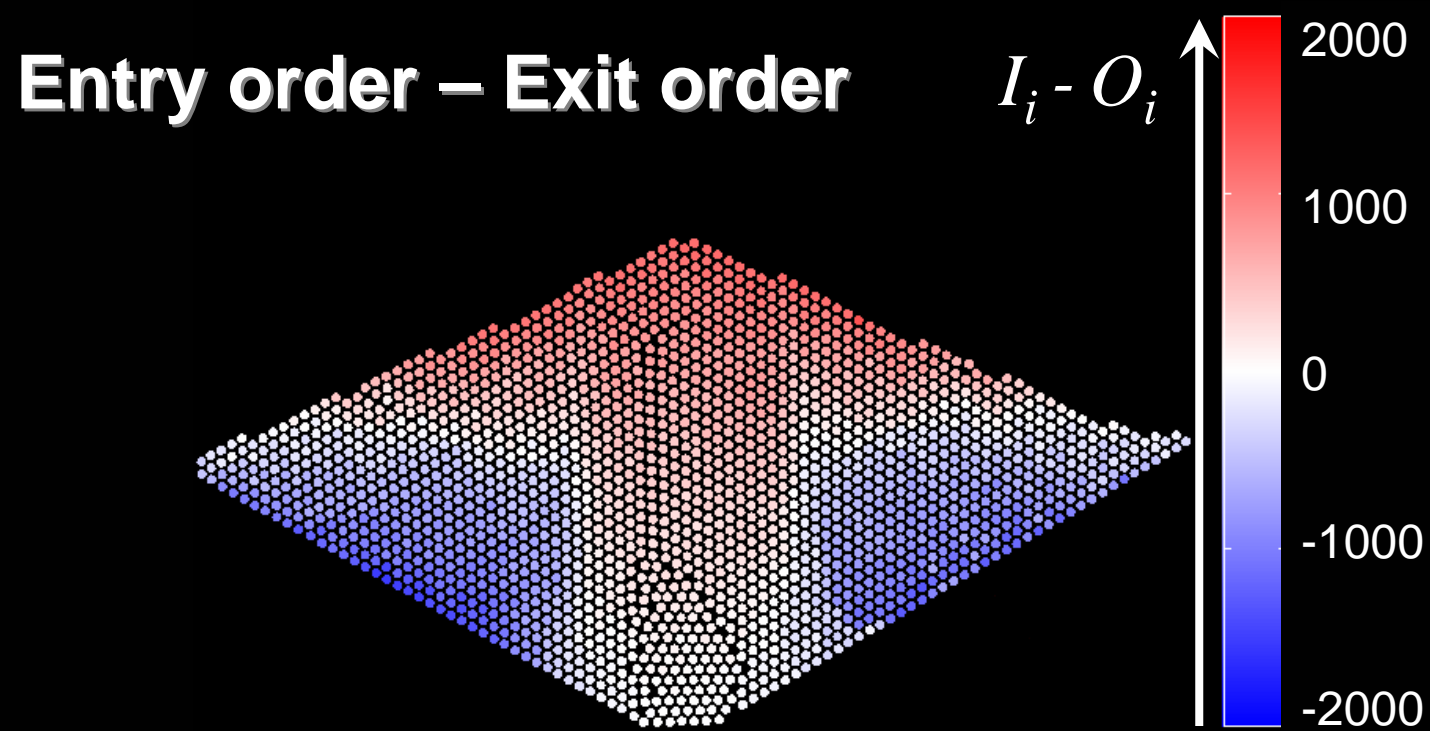
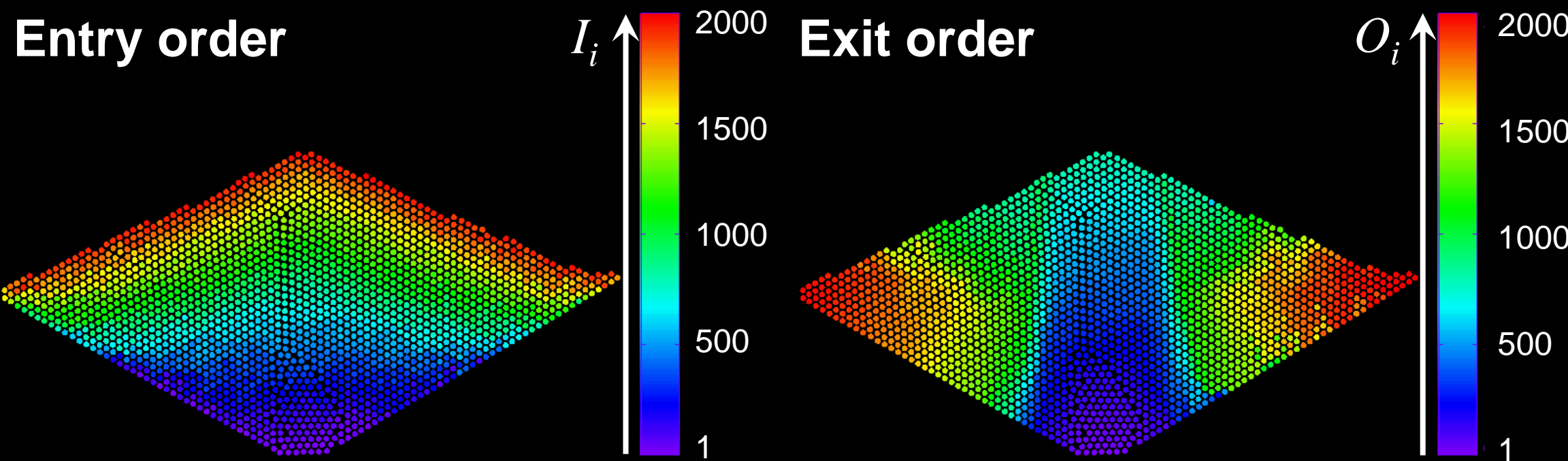


# Exit order



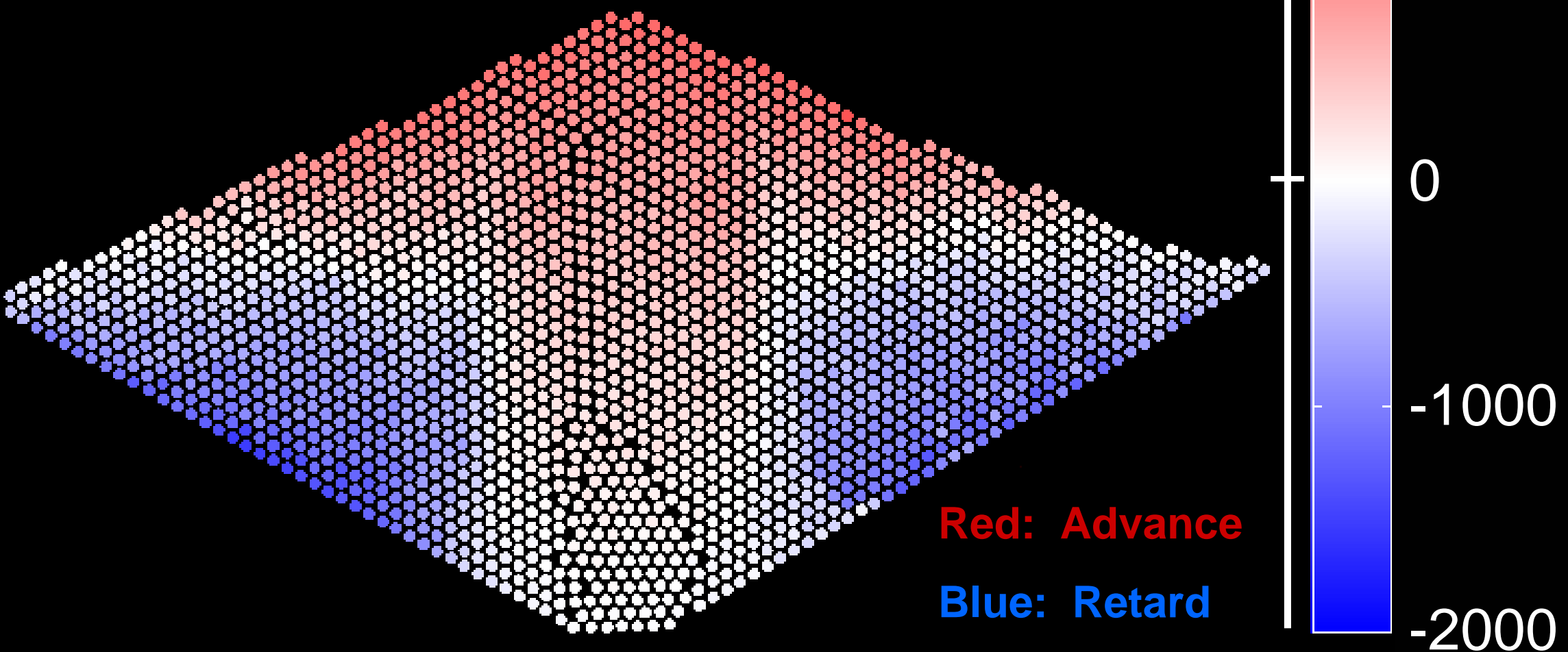
# Exit order





$$\gamma_i = I_i - O_i \rightarrow \text{ID}$$

Entry Order      Exit Order

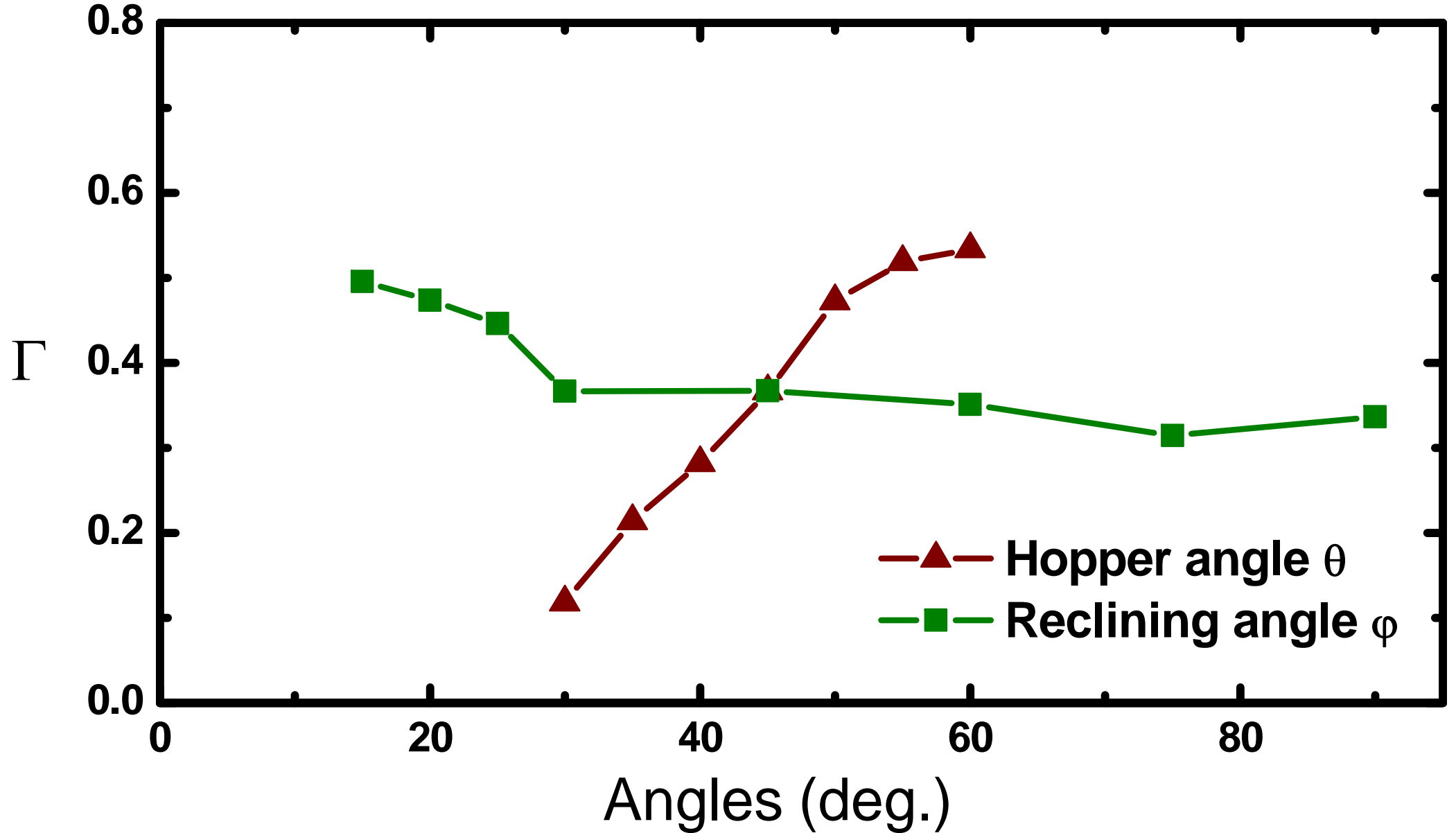


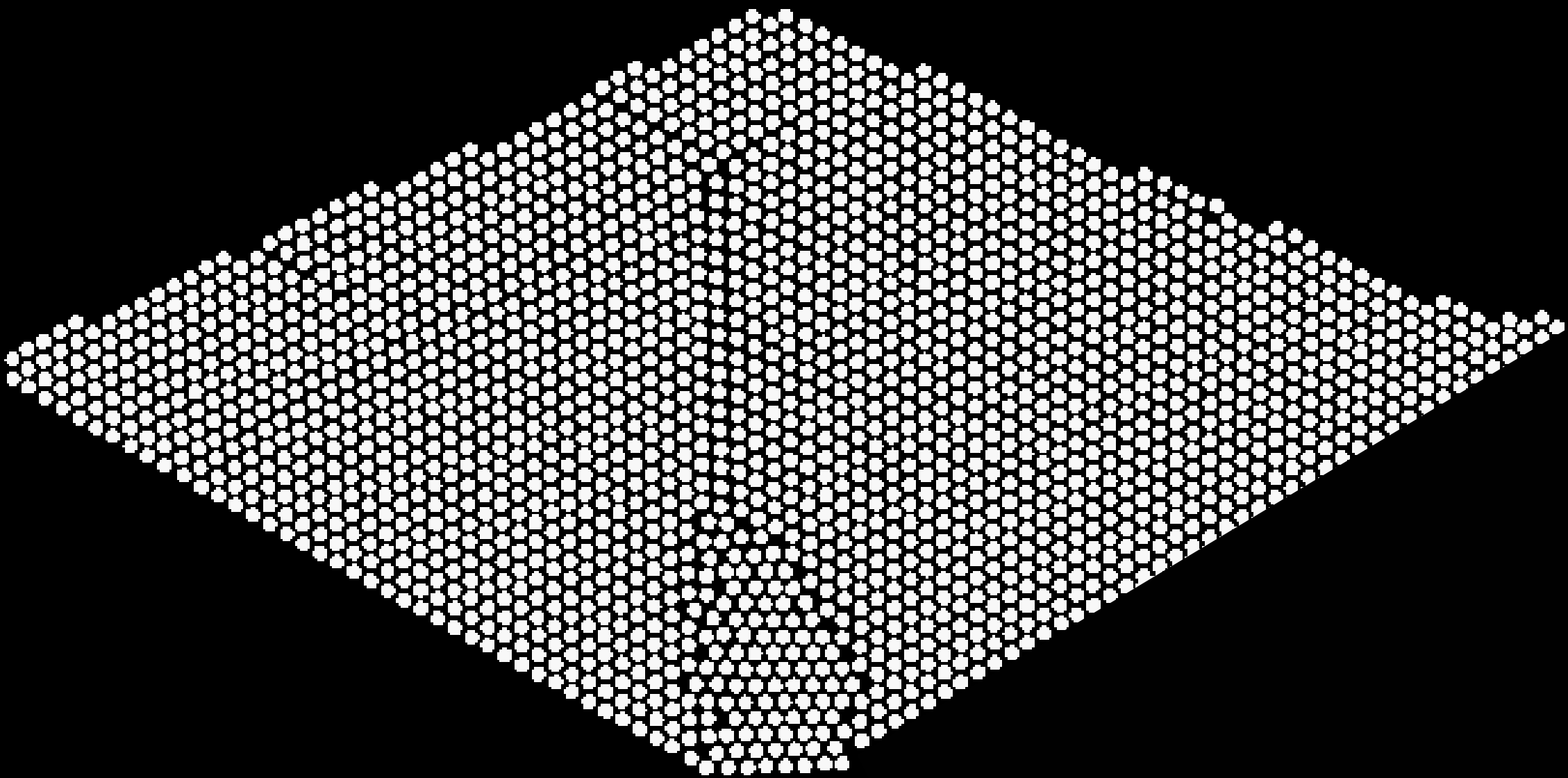
**Degree of  
reverse ordering**

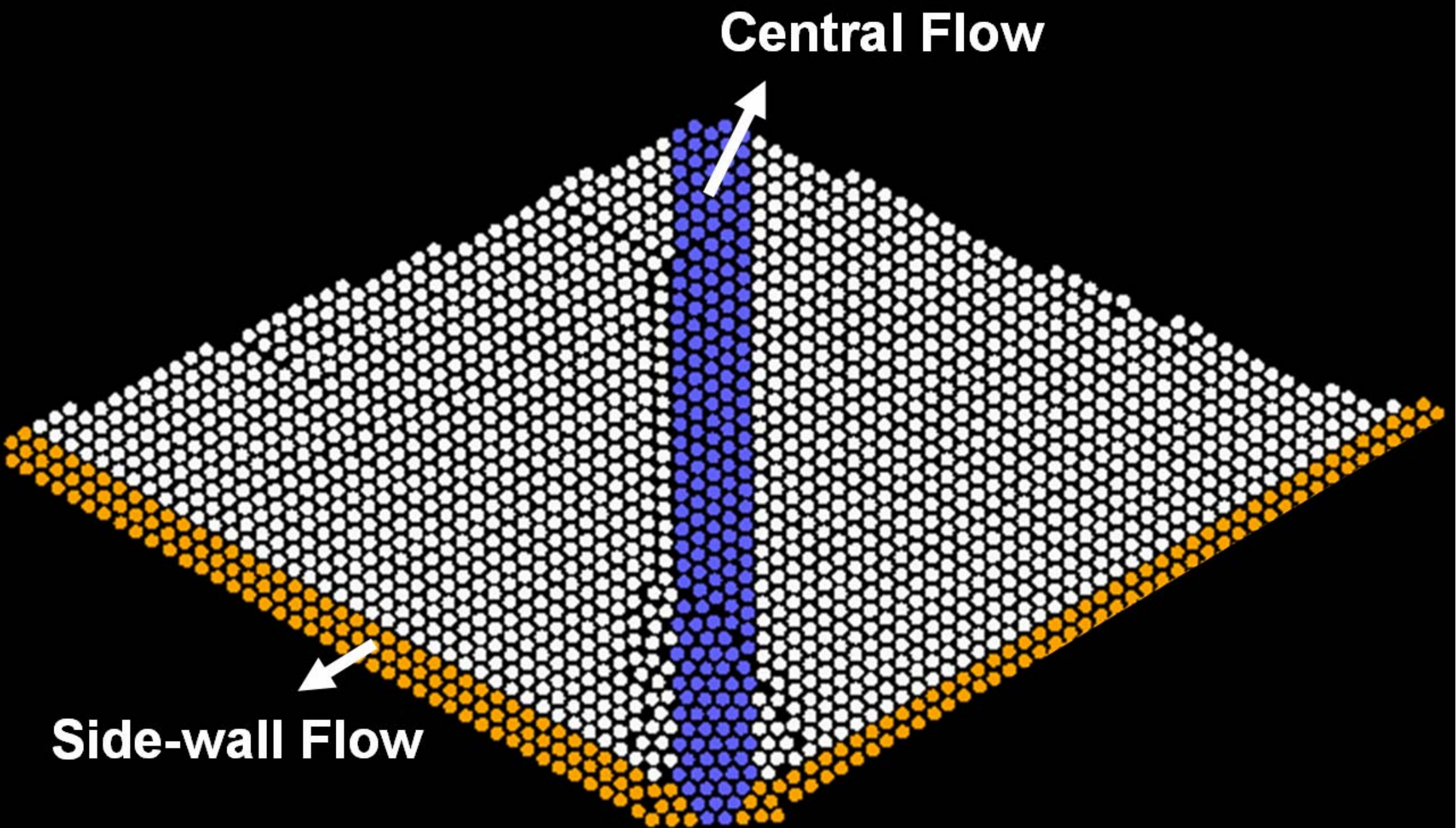
$$\Gamma = \frac{1}{f(N)} \sqrt{\sum_{i=1}^N \gamma_i^2}$$



# Hopper angle / Reclining angle and $\Gamma$







**Central Flow**

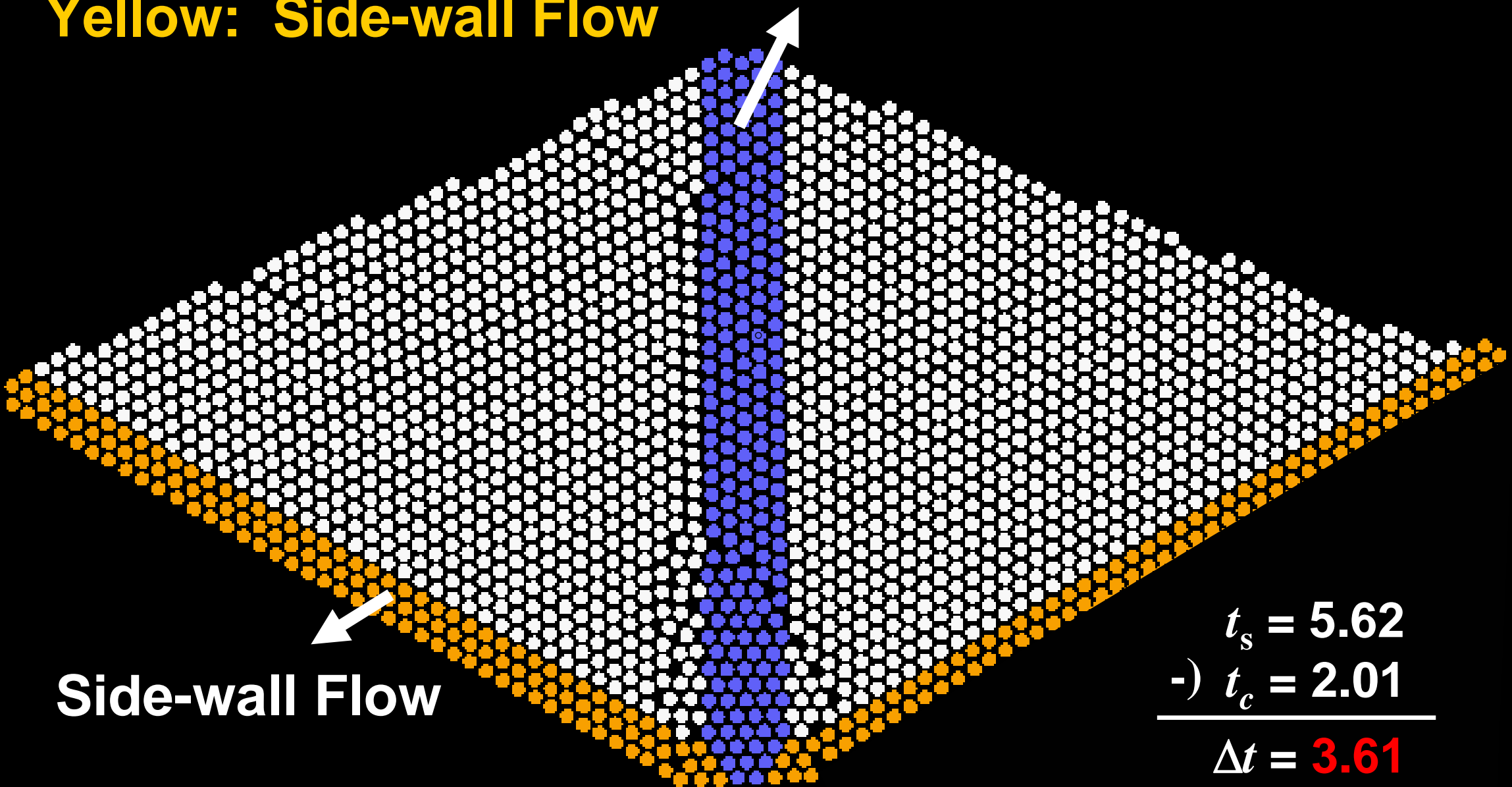
**Side-wall Flow**



**Blue: Central Flow**

**Yellow: Side-wall Flow**

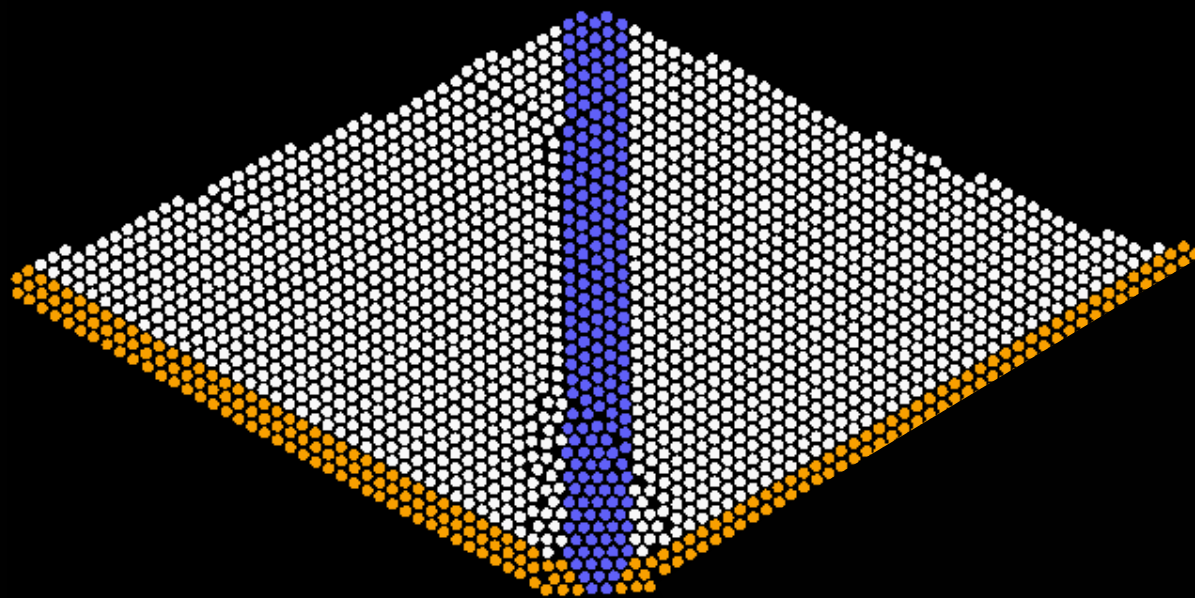
**Central Flow**



**Side-wall Flow**

$$\begin{array}{r} t_s = 5.62 \\ -) t_c = 2.01 \\ \hline \Delta t = 3.61 \end{array}$$

$\theta = 60^\circ$

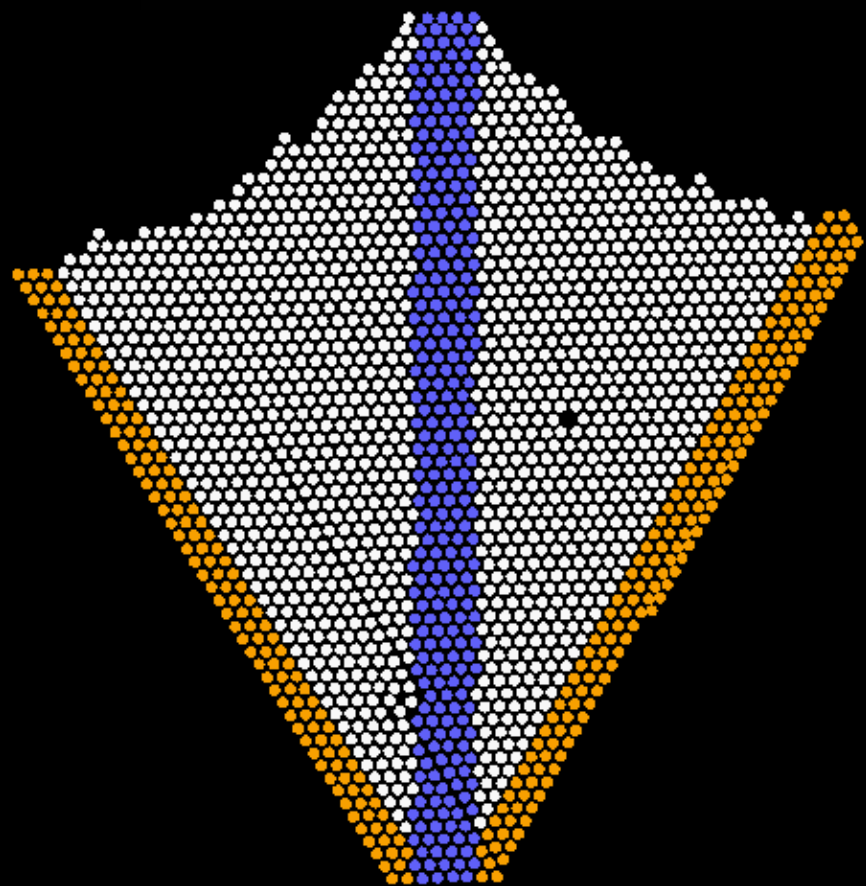


$$t_s = 5.62 \quad t_c = 2.01$$

$$\Delta t = 3.61 \text{ (sec.)}$$

$$\Gamma = 0.53$$

$\theta = 30^\circ$



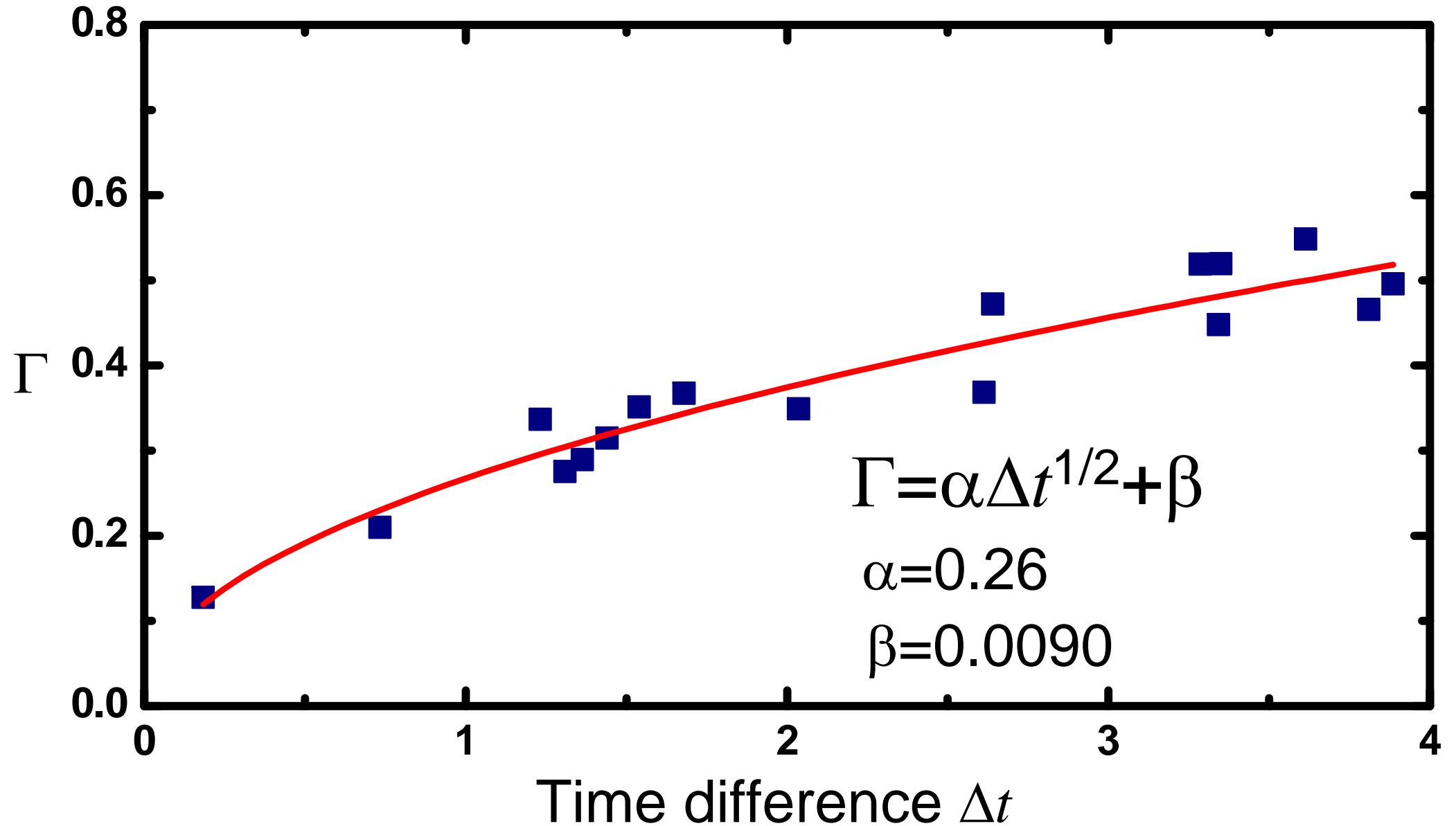
$$t_s = 3.80 \quad t_c = 3.62$$

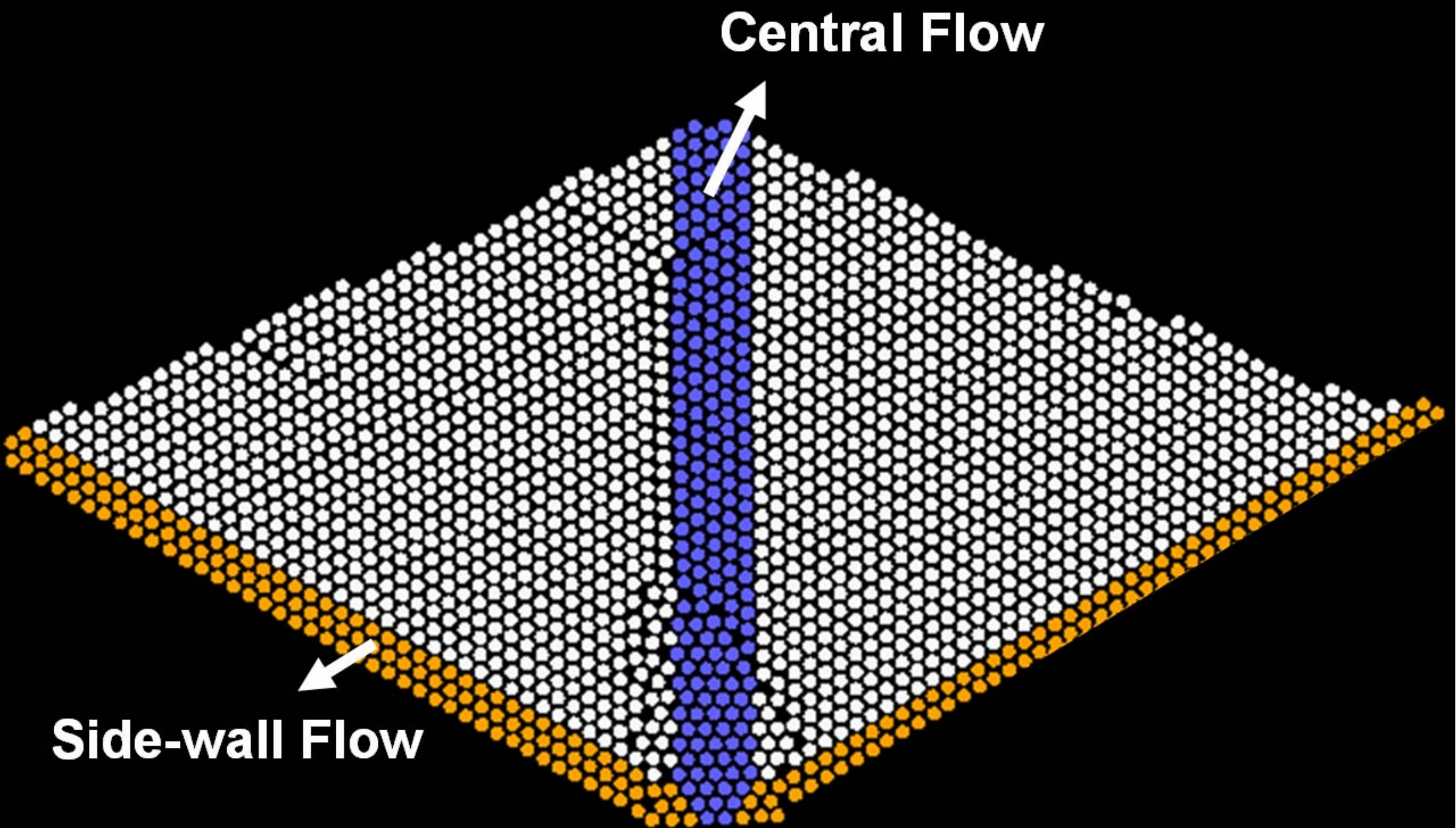
$$\Delta t = 0.18 \text{ (sec.)}$$

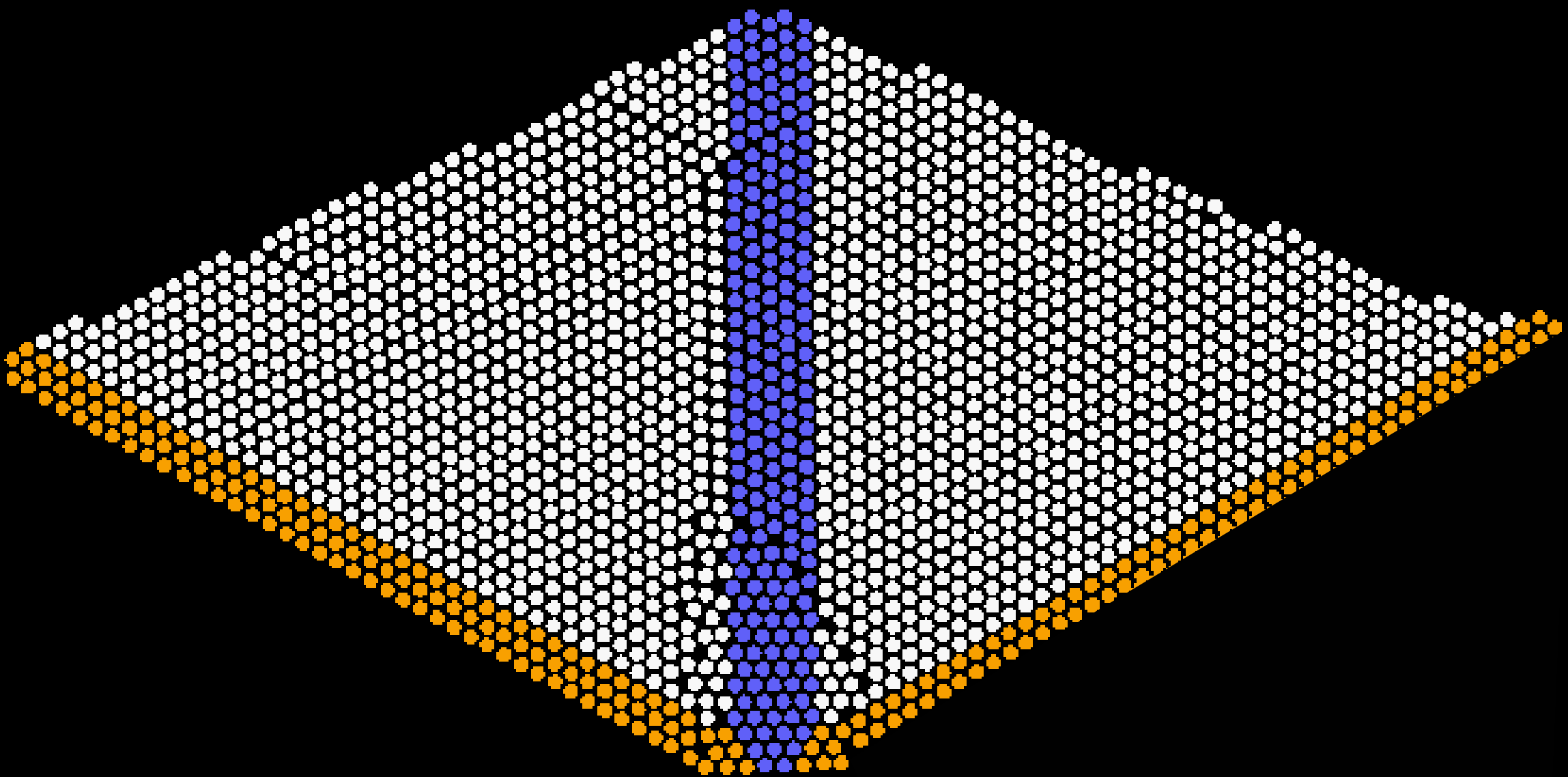
$$\Gamma = 0.12$$

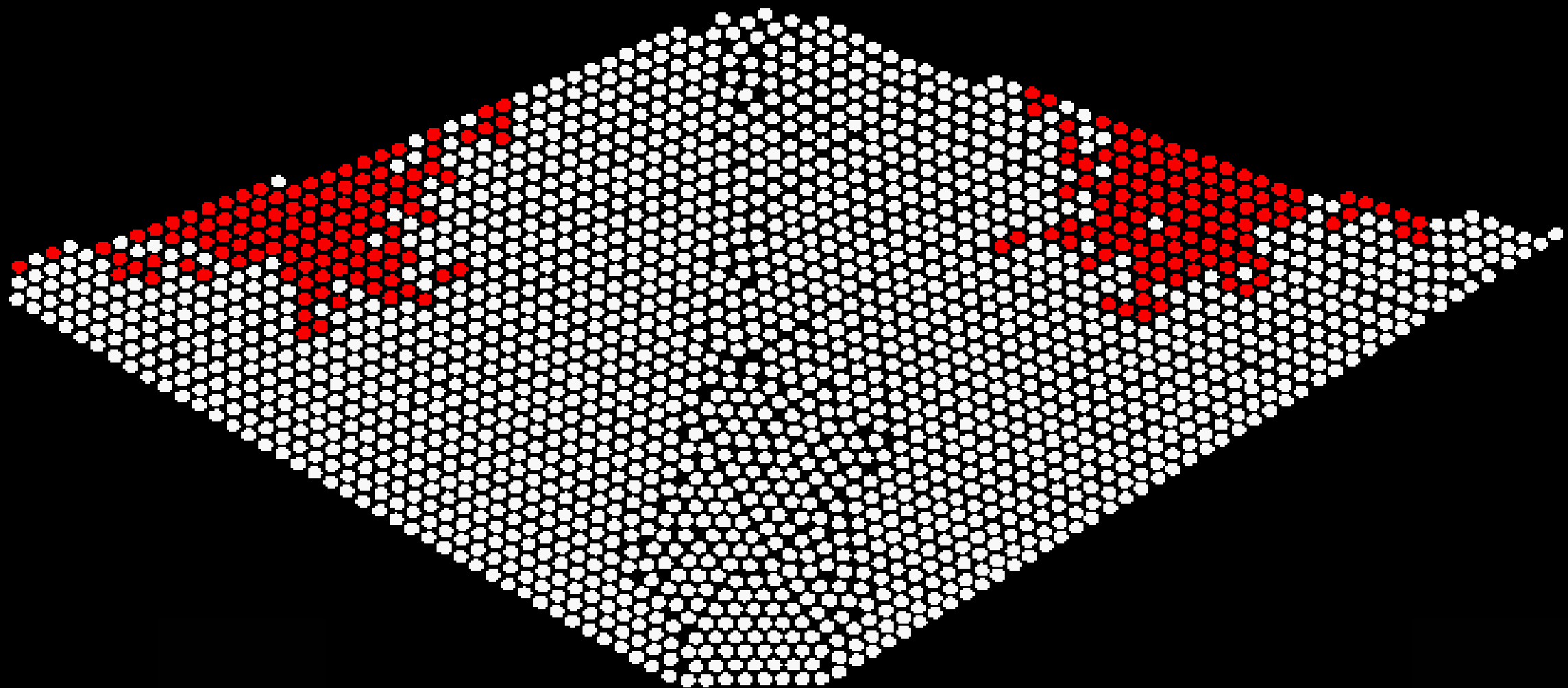
Not in real time.

# Relation between $\Gamma$ and the time difference

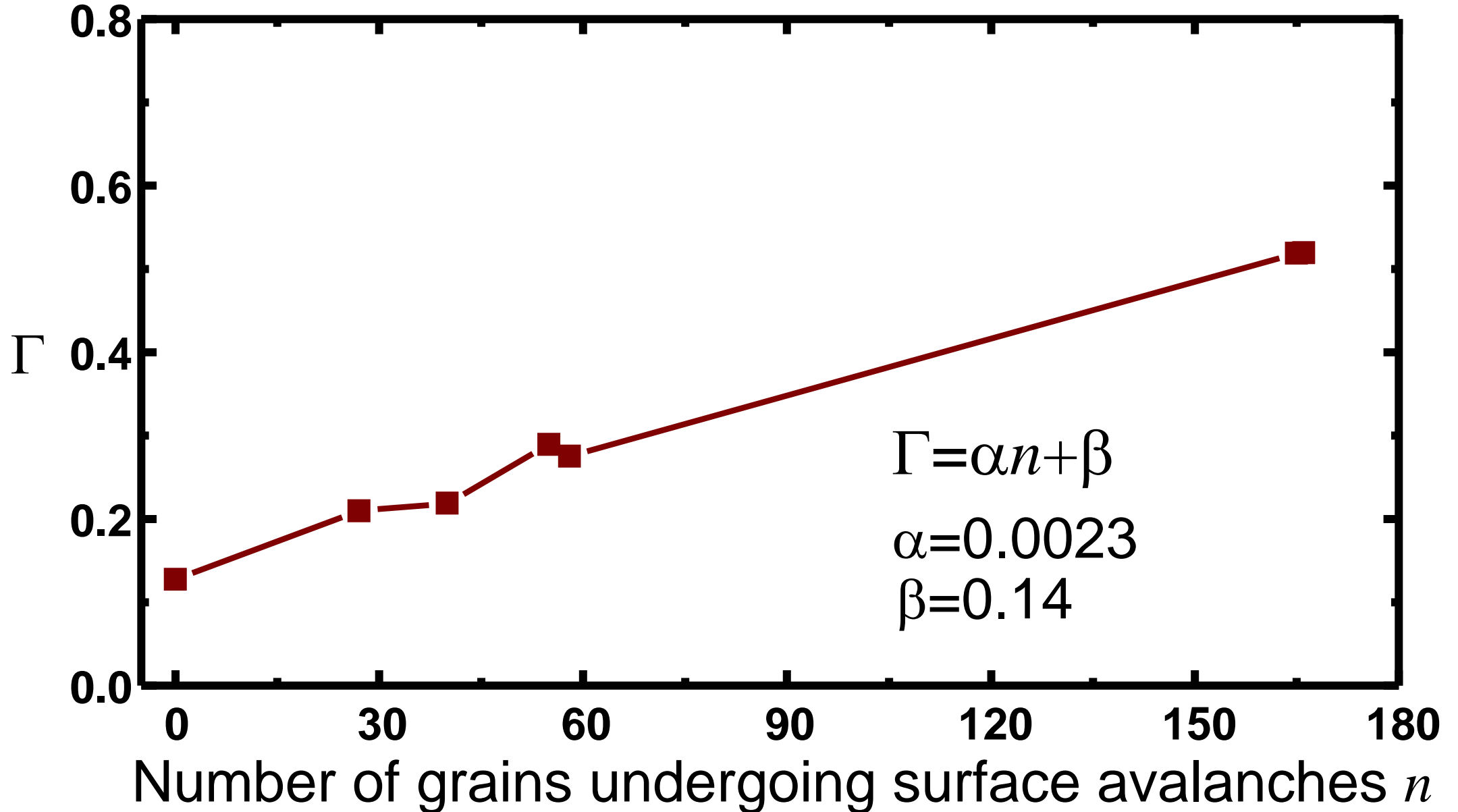






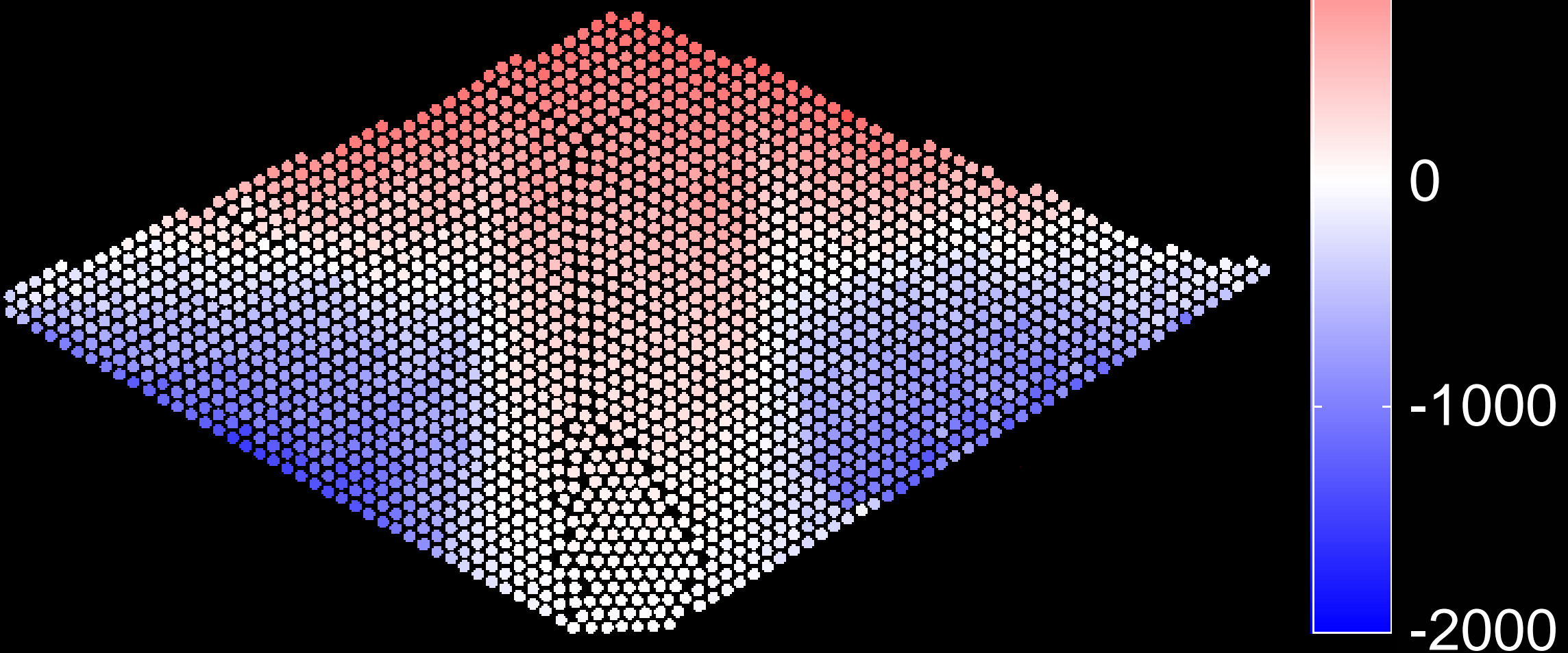


# Relation between $\Gamma$ and avalanches





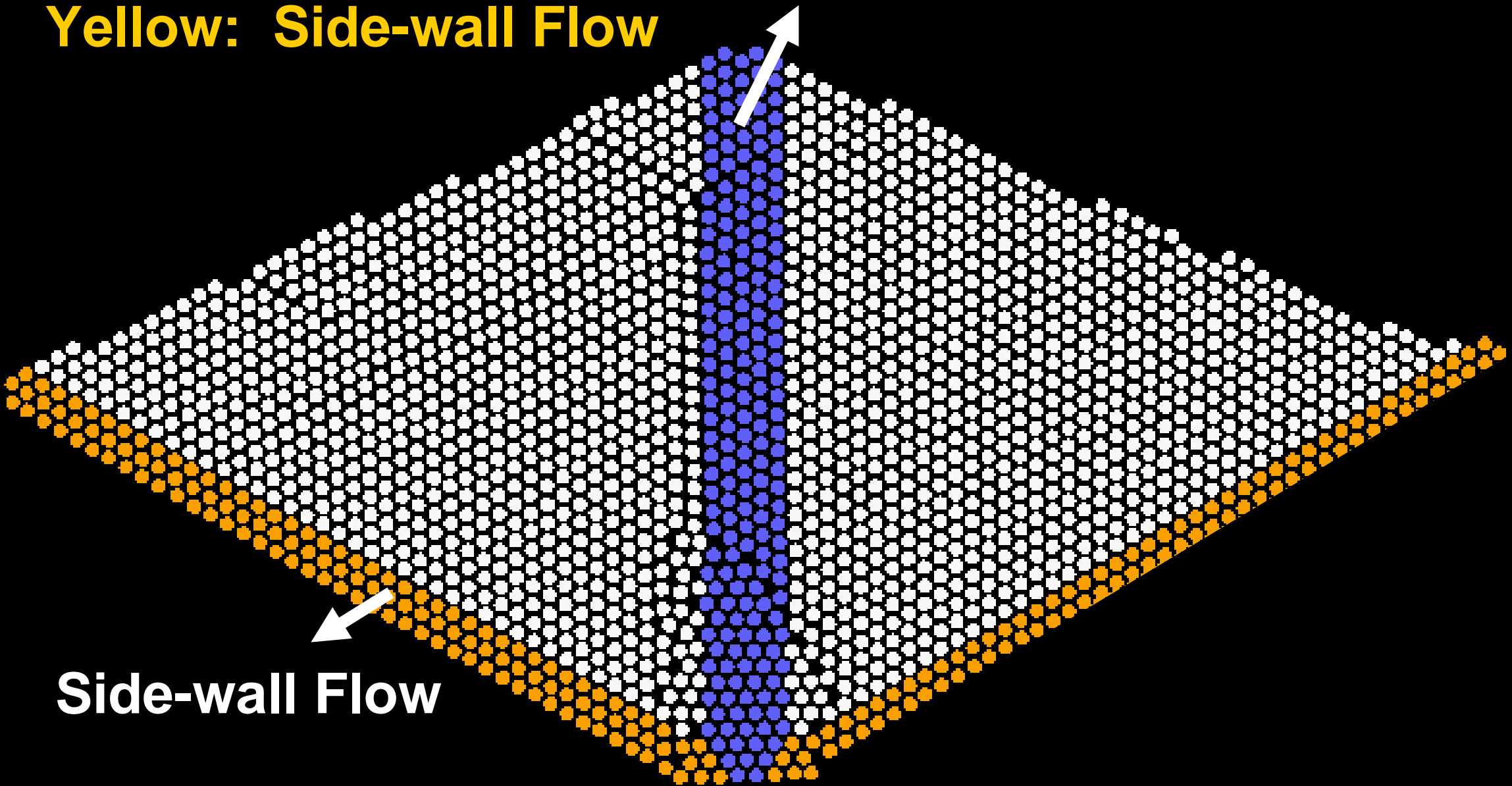
$$\Gamma = \frac{1}{f(N)} \sqrt{\sum_{i=1}^N \gamma_i^2}$$



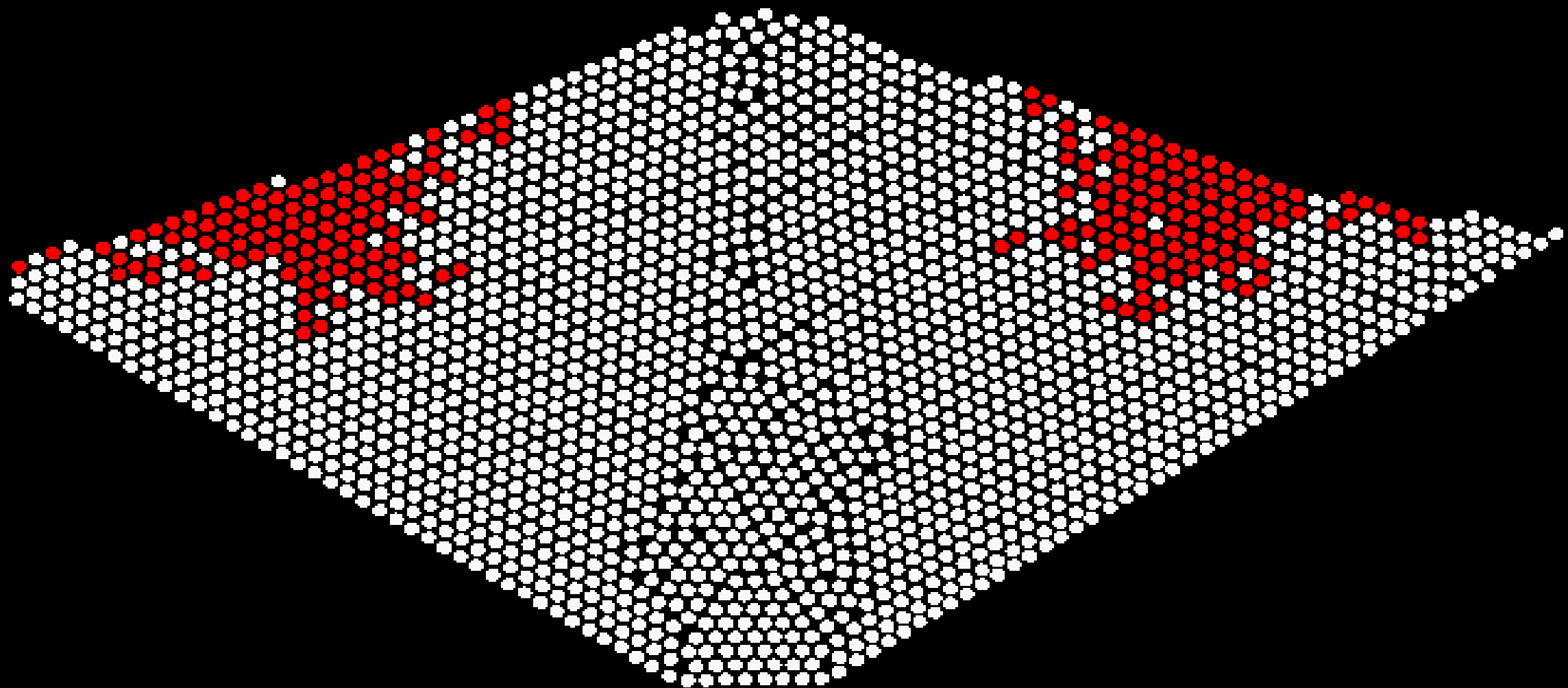
**Blue: Central Flow**

**Yellow: Side-wall Flow**

**Central Flow**



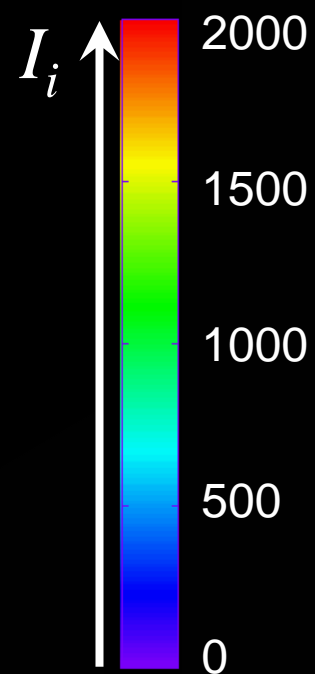
**Side-wall Flow**



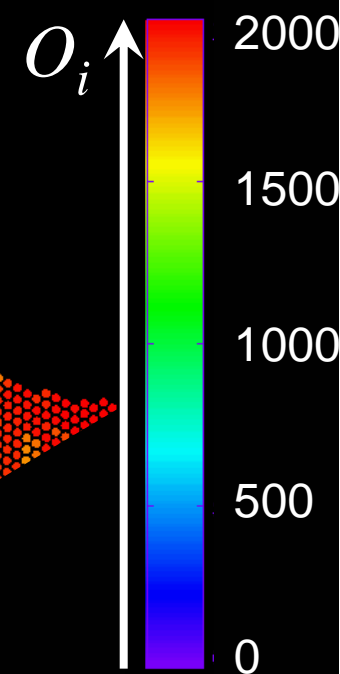
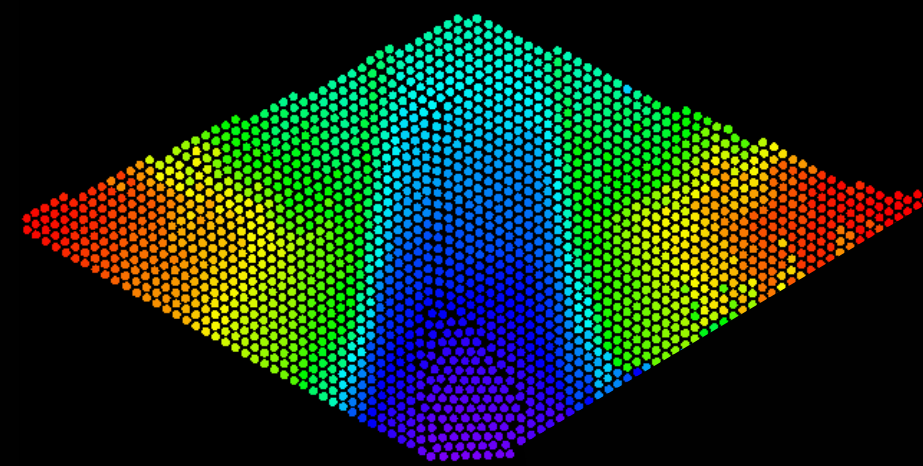
# References

- [1] T. Nguyen, C. Brennen, R. Sabersky (1980). Funnel Flow in Hoppers. *Journal of Applied Mechanics*, 102 (4). pp. 729-735.
- [2] M. Hou, W. Chen, T. Zhang, K. Lu, C. K. Chan (2003). Global nature of dilute-to-dense transition of granular flows in a 2D channel. *Phys. Rev. Lett.*, 91. pp. 204301.

**Entry order**



**Exit order**



**Entry order – Exit order**

